

ENGINEERING & MANAGEMENT EXAMINATIONS, JUNE - 2009 OPERATIONS RESEARCH AND OPTIMIZATION TECHNIQUES SEMESTER - 4

	Graph sheets are pr	rovided at the	e end of the booklet.	
		GROUP - A		
	(Multiple (Choice Type	Questions)	
Cho	pose the correct alternatives for	r any ten of t	he following :	$10 \times 1 = 10$
1)	Given a system of m simi	ultaneous eq	uations in n unknow	ns $(m < n)$, the
•	number of basic variables w	rill be		
	a) m	b)	n	
7 1	c) m-n	d)	m+n.	
ii)	A two-person zero-sum gam	e is said to b	e fair if	
	a) both the players have	equal numbe	r of strategies	
	b) the game has a saddle	point		
	c) the game does not have	ve a saddle po	int	
	d) the value of the game	is zero.		
iii)	In an assignment problem	involving f	our workers and thre	e jobs, the total
	number of assignments poss	sible is		
	a) 4	b)	3	
	c) 7	d)	21.	
ív)	In { (M/M/1) : (~ /F/FO)	l. average len	gth of a non-empty gu	eue is
	a) $\frac{\lambda^2}{\mu (\mu - \lambda)}$	b)	<u>u</u> u-λ	
			$\mu + \lambda$	
	c) $\frac{\lambda \mu}{(\mu - \lambda)^2}$	d)	none of these.	
v)	In a flow pattern $\Sigma f_{tA} = \Sigma f_{At}$	when the ve	rtex A is	
	a) arbitrary vertex	b)	any vertex other tha	n source
	transfer for the second of	d)	none of these.	



vi)	The formula for finding the minimum inventory cost under the purchasing mode
	without shortage is

a)
$$\sqrt{2RC_1C_3}$$

b)
$$\frac{\sqrt{2C_3R}}{C_1}$$

c)
$$\frac{\sqrt{C_1}}{2RC_3}$$

d) none of these.

vii) A simplex in two dimension is

a) rectangle

b) line segment

c) triangle

d) pentagon.

viii) When a positive quantity R is divided into five parts, the maximum value of their product is

a) 5k

b) (k/5)⁵

c) (k5)5

d) 5 (k/5).

ix) The optimality condition for minimization LPP in the simplex method is

a) $Z_j - C_j \ge 0$

b) $Z_J - C_J \le 0$

c) $Z_J - C_J < 0$

d) none of these.

x) What is the method used to solve an LPP involving artificial variables?

- a) Simplex method
- b) Charnes M method

c) VAM

d) None of these.

xi) Consider the following game :

Player (A)

Player (B)

	1	2	3
1	. 5	50	50
2	1	. 1	0.1
3	10	1	10

Then the value of the game is

a) $\frac{10}{3}$

b) $\frac{50}{7}$

c) 55

d) 50.



The total number of possible solutions for nxn assignment problem is always xii)

a)

c) 1

The point of intersection of pure strategies in a game is called xiii)

- value of the game a)
- saddle point b)
- c) mixed strategy
- d) optimal strategy.

The system of simultaneous equations given by xiv)

$$2x_1 + 3x_2 + 4 = 0$$

$$3x_1 + 4x_2 + 6 = 0$$

$$4x_1 + 5x_2 + 8 = 0$$

is \

a) consistent

- inconsistent b)
- possessing unique solution c)
- none of these.

GROUP - B

d)

(Short Answer Type Questions)

Answer any three of the following.

Solve the following LPP by graphical method:

$$Z = 20 x_1 + 10 x_2$$

Subject to
$$x_1 + 2x_2 \le 40$$

$$3x_1 + x_2 \ge 30$$

$$4x_1 + 3x_2 \ge 60$$

$$x_1, x_2 \ge 0$$



- 3. Arrivals at a telephone booth are considered to be Poisson with an average time of 10 minutes between one arrival and the next. The length of the phone call is assumed to be distributed exponentially with mean 3 minutes.
 - i) What is the prolability that a person arriving at the booth will have to wait?
 - ii) The telephone department will install a second booth when convinced that an arrival would expect waiting for at least 3 minutes for a phone call. By how much should the flow of arrivals increase in order to justify a second booth?
 - iii) What is the average length of the queue that forms time to time?
- 4. Find the optimal strategies and the value of the game G whose pay-off matrix is

	Play	er B
Player A	- 2	6
de la	. 5	1

5. There are five jobs, each of which is to be processed through two machines M_1 and M_2 in the order M_1 M_2 . The processing hours are the following:

Jobs	1	2	3	4	5
M ₁	3	8	5	7	4
M ₂	4	10	6	5	8

Determine the optimal sequence of the five jobs, the minimum elapsed time and the ideal times for the machines M_1 and M_2 .

6. Find the basic solution or solutions, if there be any, of the set of equations

$$2x_1 + 4x_2 - 2x_3 = 1$$
$$10x_1 + 3x_2 - 7x_3 = 33$$

7. Solve the assigment problem:

	1	2	3
A	7	5	6
В	8	4	7
C	9	6	4



GROUP - C

(Long Answer Type Questions)

Answer any three questions.

 $3 \times 15 = 45$

. a) Solve the following LPP by Simplex method.

3 A 10 = 40

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 $Maximize Z = 60x_1 + 50x_2$

subject to

$$x_1 + 2x_2 \le 40$$
$$3x_1 + 2x_2 \le 60$$

$$x_1, x_2 \ge 0$$

b) Solve the following linear programming problem by Charnes Big M method (if possible):

Maximize $Z = 2x_1 - x_2 + 5x_3$

subject to

$$x_1 + 2x_2 + 2x_3 \le 2$$

$$\frac{5}{2}x_1 + 3x_2 + 4x_3 = 12$$

$$4x_1 + 3x_2 + 2x_3 \ge 24$$

and
$$x_1$$
 , x_2 , $x_3 \ge 0$

What is the optimal value of Z?

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9. a) Write down the dual of the following LPP:

$$Minimize Z = 3x_1 + x_2$$

subject to

$$2x_1 + x_2 \ge 14$$
,

$$x_1 - x_2 \ge 4$$
, x_1 , $x_2 \ge 0$,

and solving the dual problem find out the optimal solution and the optimal value of the objective function.

b) Find the optimal solution to the following integer programming problem: 7

 $Maximize Z = x_1 - x_2$

subject to $x_1 + 2x_2 \le 4$,

$$6x_1 + 2x_2 \le 9$$
, x_1 , $x_2 \ge 0$ and

 x_1 , x_2 are integers.



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10. a) Solve the following balanced Transportation Problem:

	D_1	D ₂	D ₃	D_4	Capacity
Fl	2	3	11	7	6
F2	1	0	6	1	1
F3	5	8	15	9	10
Requirement	7	5	3	2	17

b) Use dynamic programming to solve the following problems:

Minimize
$$Z = y_1^2 + y_2^2 + y_3^3$$

subject to $y_1 + y_2 + y_3 \ge 15$

and
$$y_1, y_2, y_3 \ge 0$$
.

11. a) Solve the following two-person-zero game using the method of dominance:

		Playe	rB .	
	5	- 10	9	0
Player A	6	7	8	1
	8	7	15	1 .
	3	4	- 1	4

b) Find the optimal assignments to find the minimum cost for the assignment following cost matrix:

	J1	J2	J3
P1	12	24	15
P2	23	18	24
P3	30	14	28

12. Use dynamic programming to solve

Maximum
$$Z = Y_1 \cdot Y_2 \cdot Y_3$$

Subject to constraints

$$Y_1 + Y_2 + Y_3 = 5$$

and
$$Y_1$$
, Y_2 , $Y_3 \ge 0$.

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CS/MCA/SEM-4/MM-401/09



- 13. a) Write the differences between PERT and CPM.
 - b) The following information is given:

Activity	1-2	2-3	2-4	3 - 5	4 - 6	5 - 6	5 - 7	6 - 7
Pessimistic	3	9	6	8	8	0	5	8
Most likely	3	6	4	6	6	0	4	5
Optimistic time (weeks)	3	3	2	4	4	0	3	. 3

Draw the network diagram for the above. Calculate

- i) Variance of each activity
- ii) Critical path and expected project length
- iii) The probability that the project will be completed in 23 weeks.

Given:

Z-value	1.9	1.91	1.92	1.93	1.94
		0.9719	0.9726	0.9732	0.9738
Probability	0.9713	0.9719	0.0120		

4+2+(2+1)+4

14. a) Assuming that the expected times are normally distributed, find the probability of meeting the schedule date for the given network:

Job	1 - 2	1-3	2 - 4	3-4,	4 - 5	3 - 5
t _o	2	9	5	2	6	8
t _m	5	12	14	5	6	17
t _p	14	15	17	12	12	20

Schedule project completion date is 30 days. Also find the date on which the project manager can complete the project with a probability of 0.90.



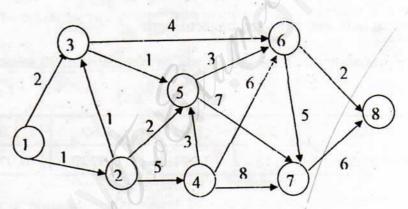
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b) A small project consists of seven activities for which the relevant data are given:

Activity	Immediate predecessors	Time (days)		
Α				
В	1 - 1 1 - 1 1 AL C	1		
С	A	3		
D	A, B			
E	C, D	1		
F	B, D	3		
G	E, F	i		

i) Draw the network diagram.

ii) Indicate the critical path and calculate the total float and free float for each activity.



b) The following table shows the jobs of a network along with their time estimates.

The time estimates are in days:

Job	1 - 2	1 - 6	2 - 9	2 - 4	3 - 5	4 - 5	5 - 8	6 - 7	7 - 8
to	3	2	6	2	5	3	1	3	4
t _m	6	5	12	5	11	6	4	9	9
tb	15	14	30	8	17	15	7	27	28

Draw the project network.

Find the critical path.

ii) Find the probability that the project is completed in 31 days. [$P(z \le -2.1667) = 0.0114$].

END