

*MASR*

- N.B.** (1) Question No. 1 is compulsory.  
 (2) Attempt any four from the remaining questions.  
 (3) **Figures to the right indicate full marks.**  
 (4) Assume suitable data whenever **required.**  
 (5) Vector notation should be used whenever **necessary.**

*1. E field & vector field. mag. fields & waves 7/11/17*

1. Attempt any four of the followings :—
  - (a) Explain the concept of conservative nature of electric field. 10
  - (b) Obtain the point form of continuity equation 10
  - (c) Explain method of images 10
  - (d) Explain the concept of scalar and vector magnetic potential 10
  - (e) Define the following term :—  
 $\eta, z_0, \gamma, \delta$ . 10
  
2. (a) The circular region,  $\rho < a, z = 0$ , carries a uniform surface charge density  $\rho_s$ . Find  $\bar{E}$  at  $(0, 0, h), h > 0$ . 10
- (b) Evaluate both sides of the divergence theorem for the region  $r \leq 2$  if  $\bar{G} = 5r \sin^2 \theta \cos^2 \phi \bar{a}_r$ . 10
  
3. (a) The volume in cylindrical coordinates between  $r = 2$  m and  $r = 4$  m contains a uniform charge density  $\rho_v$  (c/m<sup>3</sup>). Find  $\bar{D}$  in the regions using Gauss's law. 10
- (b) A square of side 1 m has a point charge  $Q_1 = 1$  pc at the upper right corner, a point charge  $Q_2 = -10$  pc at the lower right corner and a line distribution of charge  $\rho_l = 10$  pc/m along the left edge. Find  $V$  at point  $P$  at the center of the square. 10
  
4. (a) The region  $y < 0$  contains a dielectric material for which  $\epsilon_{R1} = 2.5$ , while the region  $y > 0$  is characterized by  $\epsilon_{R2} = 4$ . Let  $\bar{E}_1 = -30a_x + 50a_y + 70a_z$  v/m, and find ; 10  
 (a)  $D_{N2}$  (b)  $D_{t2}$  (c)  $\bar{D}_2$  (d)  $\bar{P}_2$  (e)  $\theta_2$ .
- (b) A filamentary current of 10 A is directed in from infinity to the origin on the positive x-axis and then back out to infinity along the y-axis. Use the Biot-Savart law to find  $\bar{H}$  at  $P(0, 0, 1)$ . 10
  
5. (a) Discuss the phenomenon of polarization in dielectric medium. Discuss how it gives rise to bound charge densities. 10
- (b) Two circular coils are located at the  $z = 0$  plane and  $z = 5$  m plane, centered about the z-axis. The first coil having a radius of 1 m carries a current of 10 Amp. The second coil having a radius of 0.5 m carries a current of 20 Amp. Calculate the magnetic field intensity  $\bar{H}$  at  $(0, 0, 2.5$  m). 10
  
6. (a) Give the general set of Maxwell's Equations in point form. Derive the set of Maxwell's Equations for static fields and harmonically time varying fields. 10
- (b) The Electric field intensity of a 300 MHz uniform plane wave in free space is given as 10  
 $\bar{E}_s = (20 + j50) (\bar{a}_x + 2\bar{a}_y) e^{-j\beta z}$  v/m,  
 (i) Find  $w, \lambda, v$  and  $\beta$ .  
 (ii) Find  $\bar{E}$  at  $t = 1$  ns,  $z = 10$  cm.  
 (iii) What is  $|\bar{H}|_{\max}$  ?
  
7. (a) Starting with Maxwell's Equations obtain vector wave equation for lossy dielectric. Solve it by considering that  $\bar{E}$  has only y-component and the wave is travelling in x-direction. Hence obtain an Expression for the complex intrinsic impedance. 12
- (b) The transmitting antenna located at the origin of co-ordinate system produces the electric field intensity  $E(r,t) = \bar{a}_r V_0 \frac{\sin \theta}{r} \cos \omega(t - r/c)$  (v/m) and the magnetic field of this antenna measured in A/m is  $H(r,t) = \bar{a}_\phi \frac{V}{377} \frac{\sin \theta}{r} \cos \omega(t - r/c)$  where 'C' is the velocity of light. 8  
 Calculate the Poynting vector the average power radiated from this antenna.