

Code.No: 09A1BS04

R09

SET-4

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD**I B.TECH – REGULAR EXAMINATIONS, JUNE - 2010****MATHEMATICAL METHODS****(COMMON TO EEE, ECE, CSE, EIE, BME, IT, ETE, E.COMP.E, ICE)****Time: 3hours****Max.Marks:80**

Answer any FIVE questions
All questions carry equal marks

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- 1.a) Find the Rank of the Matrix, by reducing it to the normal form
- $$\begin{bmatrix} 1 & 3 & 4 & 5 \\ 1 & 2 & 6 & 7 \\ 1 & 5 & 0 & 10 \end{bmatrix}$$
- b) Find whether the following system of equations are consistent. If so solve them.
 $x + 2y + 2z = 2$, $3x - 2y - z = 5$, $2x - 5y + 3z = -4$, $x + 4y + 6z = 0$. [7+8]
2. Find the eigen values and the corresponding eigen vectors of
- $$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{bmatrix}$$
- [15]
3. Reduce the quadratic form to the canonical form $3x^2 + 2y^2 + 3z^2 - 2xy - 2yz$ [15]
- 4.a) Prove that the newton's method has quadratic convergence.
b) Find $y(5)$ given that $y(0)=1$, $y(1)=3$, $y(3)=13$, and $y(8) = 123$ using Lagrange's formula. [8+7]
- 5.a) Find $\frac{dy}{dx}$ at $x=7.5$ from the following table.
- | | | | | | | | |
|---|------|------|------|------|------|------|------|
| x | 7.47 | 7.48 | 7.49 | 7.5 | 7.51 | 7.52 | 7.53 |
| y | .193 | .195 | .198 | .201 | .203 | .206 | .208 |
- b) Find the first two derivative at $x=1.4$ from the following data: [8+7]
- | | | | | | | |
|---|-----|------|------|-------|-------|-----|
| x | 1.0 | 1.2 | 1.4 | 1.6 | 1.8 | 2.0 |
| y | 0 | .128 | .544 | 1.296 | 2.432 | 4.0 |
6. Using Euler's method, solve for y at $x=2$ from $\frac{dy}{dx} = 3x^2 + 1$, $y(1) = 2$ taking step size:
a) $h = 0.5$
b) $h = 0.25$. [8+7]
- 7.a) Expand $f(x) = \cos x$ for $0 < x < \pi$ in half range sine series.
b) Find cosine and sine series for $f(x) = \pi - x$ in $[0, \pi]$. [7+8]
- 8.a) Solve $(mz - ny)p + (nx - lz)q = (ly - mx)$.
b) Solve $(x^2 - y^2 - yz)p + (x^2 - y^2 - zx)q = z(x - y)$. [7+8]