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2008-2009  
B.Sc.(HONS.) (PART-III) EXAMINATION  
( PHYSICS )  
QUANTUM MECHANICS  
(PH-303)

Maximum Marks: 40

Duration : Three Hours.

All the questions are compulsory.  
The marks are shown against the questions.

- 1.(a) Qualitatively discuss the difference between intrinsic and orbital angular momentum. Briefly discuss whether it would be correct to say that an angular momentum of  $\hbar$  must be orbital and not intrinsic. 1+1
- (b) Briefly discuss whether the product of two hermitian operators is also hermitian. 02
- (c) Prove that

$$\frac{d}{dt} \langle p_x \rangle = \left\langle -\frac{\partial V}{\partial x} \right\rangle ,$$

where the symbols have their usual meaning.

Briefly say what the equation tells us. 2+1

- 2.(a) Explain what is meant by a stationary quantal state? 01
- (b) Briefly point out that the free particle is spread out all over the space. 02
- (c) Calculate the particle flux associated with the free particle wave function  $Ae^{ikx}$  02
- (d) Normalize the one- dimensional wave function  $e^{-\alpha x}$  of a single particle, 'situated' in the region  $0 \leq x \leq +\infty$ . 02

3. Solve the one- dimensional time- independent Schrödinger equation for a one- dimensional square well potential of a finite size and depth. Obtain the condition for a bound state to occur. Tell how many levels are bound in the potential of depth  $V_0$  and size  $a$  when  $V_0 a^2 = \frac{\hbar^2}{2m}$ , where  $m$  is the mass of the particle inside it. 4+2

OR

- 3'. What is the Zero-Point Energy of the oscillator? Relate it to the Uncertainty Principle. 2+4
4. Starting from the first principles, obtain the eigen functions and the energy eigen values of the Rigid Rotator.

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Where does the Rigid Rotator occur in physical problems?

5+1

OR

- 4'(a) What is meant by the degeneracy of an energy level? 01
- (b) Discuss the degeneracy of the levels of the Rigid Rotator. 02
- (c) Obtain the number of the degenerate levels of the hydrogen- like atom for  $n = 2$ .  
Name an agency that can break the degeneracy of the levels of the hydrogen – like atom. 2 + 1

- 5.(a) Briefly tell what first led to the picture of the 'spinning' electron. 02
- (b) Write down all the relevant mutual commutators of the operators of the electron, spin components  $S_x$ ,  $S_y$  and  $S_z$  as also of a component, say  $S_z$  and  $S^2$ . 03
- (c) Briefly discuss whether the coordinate  $x$  commutes with  $S_x$ . 02

OR

- 5'(a) What is Zeeman Effect? Explain the terms Normal Zeeman Effect and Anomalous Zeeman Effect. 03
- (b) With the help of the selection rules, discuss the transitions between two hydrogen atom levels when the system is placed in either a weak or a strong magnetic field ( you may choose either the weak or the strong case). 04
- 6.(a) Define the terms : elastic scattering cross section, scattering amplitude and phase shift. 03
- (b) If  $f(\theta, \phi)$  is the unsymmetrized scattering amplitude; write down the cross section, for fermions, when the incident particle is identical with the target. Give one practical example. 3+ 1