

2008-2009  
B.Sc.(HONS.) (PART-III) EXAMINATION  
PHYSICS  
THERMAL AND STATISTICAL PHYSICS  
(PH-304)

Maximum Marks: 40

Duration : Three Hours.

Answer all questions.

The marks are shown against the questions.

The symbols have their usual meanings.

Use of calculator is permitted.

- 1.(a) Starting with the expression for the flux of  $\theta v$  molecules at a surface, derive the equation of state of an ideal gas. 05

- (b) Briefly discuss what do you understand by fluctuations and Brownian motion? 02

OR

- 1'(a) How do you define the microscopic and macroscopic cross-sections? Obtain an expression for the mean free path of gas molecules. 05

- (b) A beam of molecules of radius  $2 \times 10^{-16}$  m strikes a gas composed of molecules whose radii are  $3 \times 10^{-10}$  m. There are  $10^{24}$  gas molecules per  $\text{m}^3$ . Determine  
(i) the radius of exclusion and  
(ii) the fraction of molecules left in the beam after it travels  $10^{-6}$  m in the gas. 02

- 2.(a) Define the empirical and thermodynamic temperatures. How are the two temperatures related? 03

- (b) Derive the following thermodynamical relations: 03

$$(i) \quad C_p - C_v = \left[ \left( \frac{\partial u}{\partial v} \right)_T + p \right] \left( \frac{\partial v}{\partial T} \right)_p$$

$$(ii) \quad \left( \frac{\partial u}{\partial T} \right)_p = C_p - pv\beta$$

- 3.(a) State the Clausius and the Kelvin-Planck statements of the second Law and show that the two statements are equivalent. 04

- (b) Sketch a Carnot cycle for an ideal gas on a (i) T-S diagram and (ii) u - v diagram. 02

- 4.(a) Discuss the porous plug experiment and draw the isenthalpic curves and inversion curve for a gas. Show that the Joule-Kelvin coefficient for a gas is given by

-2-

$$\mu = \frac{1}{C_p} \left[ T \left( \frac{\partial v}{\partial T} \right)_p - v \right]$$

What is the importance of this experiment in liquefaction of gases?

2+3+1

OR

- 4'(a) Define the first order and the second order phase transitions and obtain the Clapeyron equation.

04

- (b) Derive the following Maxwell's relations

03

$$\left( \frac{\partial P}{\partial T} \right)_v = \left( \frac{\partial S}{\partial v} \right)_T$$

$$\left( \frac{\partial v}{\partial T} \right)_p = - \left( \frac{\partial S}{\partial P} \right)_T$$

- 5.(a) Define the ensemble, the micro and macro-states and the thermodynamic probability.

02

- (b) What is the statistical definition of entropy? Show that the entropy of a system is given by

$$S = K \ln \Omega,$$

where  $\Omega$  is the thermodynamic probability of the system.

05

6. What is a quantised linear oscillator? Show that the partition function for an assembly of such oscillators is given by

$$Z = \frac{\exp(-\theta/2T)}{1 - \exp(-\theta/T)}$$

where  $\theta$  is the characteristic temperature.

07

OR

- 6'. Starting from first principles, obtain the Rayleigh-Jean formula for the black body radiation. What is the ultra-violet catastrophe?

6+1